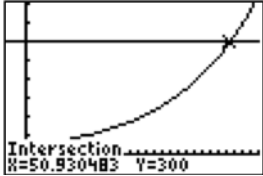


Algebra II Module 8 Lesson 13 – Solving Contextual Exponential Equations

<p>1. Your baby brother, Zach, is starting to talk and you start keeping a list of how many words he knows. When Zach was 12 months old, he had a vocabulary of 25 words and the list of words increases exponentially at a rate of 5% per <i>week</i>. Do you expect him to have a vocabulary of at least 300 words by his next birthday? Explain your answer. (Hint: Write an exponential function and evaluate that function for $x = 52$ since there are 52 weeks in a year.)</p>																	
<p>A No. Zach will only have 285 words in his vocabulary.</p>	<p>Incorrect. A <i>linear</i> function, $y = 25 + 5x$, was used to model the growth for $x = 52$, then you would get 285 words.</p>																
<p>B No. Zach will only have less than 30 words in his vocabulary.</p>	<p>Incorrect. The correct exponential equation $y = 25(1 + 0.05)^x$ was used but 2 was substituted in for x, thinking Zach would be 2 years old. The growth rate is per <i>week</i>.</p>																
<p>C There is not enough information to make a determination.</p>	<p>Incorrect. There is enough information.</p>																
<p>D Yes. Zach's vocabulary will exceed 300 words by the time he turns two.</p>	<p>Correct. The following functions were entered into the calculator: $y_1 = 25(1 + .05)^x$ and $y_2 = 300$.</p> <div style="display: flex; justify-content: space-around; margin-top: 20px;"> <div style="text-align: center;"> <p>Using the table, after 52 weeks, Zach's vocabulary would exceed 300 words:</p> <table border="1" style="border-collapse: collapse; text-align: center; font-family: monospace;"> <thead> <tr> <th>X</th> <th>Y1</th> </tr> </thead> <tbody> <tr><td>52</td><td>316.07</td></tr> <tr><td>53</td><td>331.87</td></tr> <tr><td>54</td><td>348.47</td></tr> <tr><td>55</td><td>365.89</td></tr> <tr><td>56</td><td>384.19</td></tr> <tr><td>57</td><td>403.39</td></tr> <tr><td>58</td><td>423.56</td></tr> </tbody> </table> <p>X=52</p> </div> <div style="text-align: center;"> <p>Using the multi-graph method, Zach's vocabulary will reach 300 words in under 51 weeks:</p>  </div> </div>	X	Y1	52	316.07	53	331.87	54	348.47	55	365.89	56	384.19	57	403.39	58	423.56
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